

#7 from warm up:

$$n = 2000$$

$$\hat{p} = \frac{1365}{2000}$$

$$z^* = 1.96$$

95%

$$\hat{p} = \frac{x}{n}$$

$$0.6825 \pm 1.96 \sqrt{\quad}$$

$$*\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$(0.6621, 0.7029)$$

\* I am 95% conf....

Ex. 3

$$\hat{p} = \frac{3314}{17096}$$

$$z^* = 1.65$$

$$n = 17,096$$

90% conf.

$$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$(0.18887, 0.19882)$$

$$18.9\% - 19.9\%$$

90%  
1.65

$$18.8\% - 20\%$$

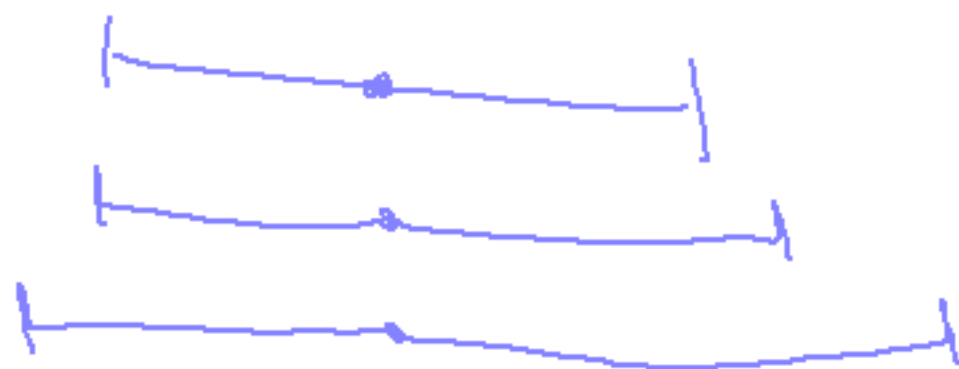
95%  
1.96

$$18.6\% - 20.2\%$$

99%  
2.58

90%

95%



Ex 5:

$$\hat{p} = 0.36$$

$$n = 50$$

$$C = 95\%$$

$$22.7\% - 49.3\%$$

$$n = 50$$

$$28.3\% - 43.7\%$$

$$n = 150$$

$$31.8\% - 40.2\%$$

$$n = 500$$

$$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

- as  $n \uparrow$ ,  
interval / margin of error  $\downarrow$

- as conf  $\uparrow$   
interval / moe  $\uparrow$

## Margin of Error:

① Small

②  $m.o.e. = Z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

③  $n$  = sample size

$Z^*$  = level of confidence

④ Confidence ( $z^*$ )  $\rightarrow$  lower

NO

Sample size  $\rightarrow$  bigger

YES

## Choosing sample size

① to give us a certain m.o.e.

②  $m = z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

← solve

③

- $m$

- $z^*$

- $\hat{p}$

\* PROBLEM:

$$\hat{p} = \frac{x}{n}$$

\* ANSWER: use a <sup>previous</sup> guess for  $\hat{p}$

④ Use a conservative value for  $\hat{p}$

$$\hat{p} = 0.50$$

Ex:  $0.03 = m$

$$95\% \rightarrow z^* = 1.96$$

$$\hat{p} = 0.50$$

$$m = z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$\frac{0.03}{1.96} = \frac{1.96 \sqrt{\frac{(0.5)(0.5)}{n}}}{1.96}$$

$$0.01531^2 = \sqrt{\frac{(0.5)(0.5)}{n}}^2$$

$$n \cdot 2.343 \times 10^{-4} = \frac{(0.5)(0.5)}{A} \cdot A$$

$$\frac{n \cdot (2.343 \times 10^{-4})}{2.343 \times 10^{-4}} = \frac{(0.5)(0.5)}{2.343 \times 10^{-4}}$$

\*ALWAYS  
ROUND  
UP

$(0.5)(0.5) / \text{Ans}$

$$n = 1067.11$$

$$n = 1068$$



$$① \quad 0.04 = 1.65 \sqrt{\frac{(0.6)(0.4)}{n}}$$

$$n = 409$$

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$$② \quad 0.01 = 2.58 \sqrt{\frac{(0.5)(0.5)}{n}}$$

$$n = 16641$$

worksheet examples